
Some aspects of Test Data Selection from Formal Specifications

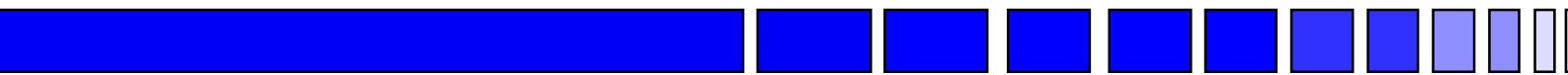
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Plan



- Main difficulties
- Contributions of formal methods
- Probabilistic approach
- Deterministic approach
- Focus on Lustre specifications

Introduction



Object : to check *adequacy / inadequacy*
between :

- the system under test
- the specification reference object

Activities of testing :

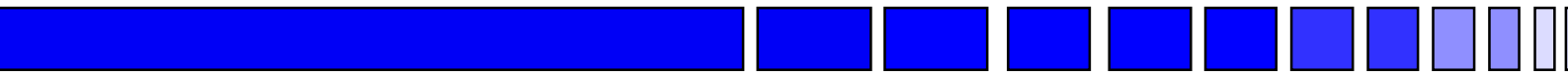
- selection of test cases
- execution of tests
- success / failure decision

Selection



- functional
- or
- structural
 - ➔ domain → subdomains
- or
- deterministic
- or
- probabilistic
 - ➔ coverage criteria

Test execution



- good modularity
- adequate entry points
- adequate observation points
- instrumentation

strong
connection



➔ impact on the early specifications

Success/failure decision (Oracle)

Predictions of the expected outputs ?

→ formal specifications can solve the problem

Other difficulties:

■ the software gives not enough observations

■ the specification says nothing

■ the specification says nothing usable

→ increase the number and the size of test case

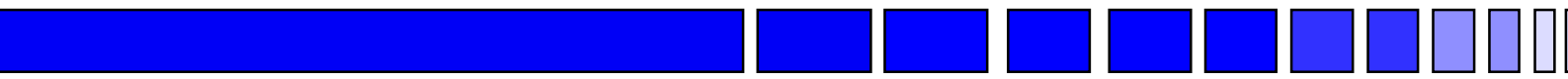
Quantitative issues



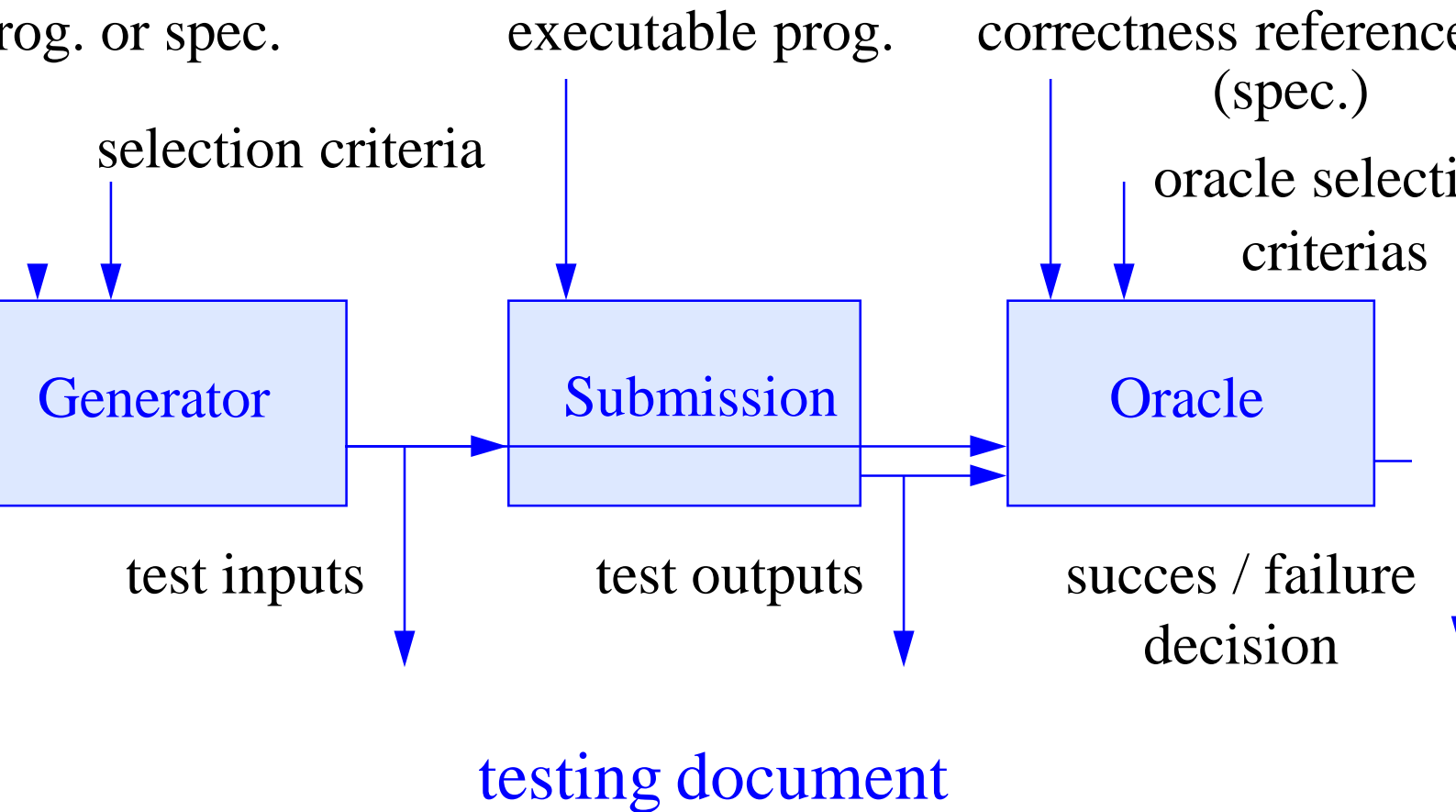
" I guarantee that the rate of failure will be less than ε "

Is a non-sense without a risk α to be wrong w.r.t. this affirmation.

Formal specifications can let you save money

- 
- cost of 1 test \approx 1/2 engineer day
 - computer aided selection and oracle $<$ 1 min
 - automatic manipulations
 - ➔ require formal specifications

Testing automation



What is a formal specification ?



■ program interface
description

$\text{sorted} : \text{List} \rightarrow \text{Bool}$

■ properties

$\text{sorted}([\]) = \text{true}$

$\text{sorted}([x]) = \text{true}$

$\text{sorted}([x, y \mid L]) =$

$(x \leq y) \text{ and } \text{sorted}([y \mid L])$

What is a formal test ?

test = formula without variable

operation(inputs) = output

sorted([1, 2, 3]) = true

much better:

observable formula deduced from the specification

sorted([1, 2, 3]) = $(1 \leq 2)$ and sorted([2, 3])

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Probabilistic testing

= the vendor affirms to the client "at most $N\varepsilon$ failures for N input values"

= the risk that the vendor takes with this affirmation (over 100 test sets of N tests, almost surely less than 100α test sets may have more than $N\varepsilon$ failures)

$$N \geq \log(\alpha) / \log(1 - \varepsilon)$$

Choice of the test cases

How to produce the N relevant test cases:

= a **complete** distribution on the domain of variables (has to be discussed with the client)

problems:

- to formalize the discussion into μ
- to generate test cases according to μ

To automate the probabilistic test

A prototype of generator

- generates tests from a set description of domains of variables (cartesien product, union, recursive definition ...)
- hides probabilistic manipulations behind set descriptions: offers default distributions.

Advantages of probabilistic testing

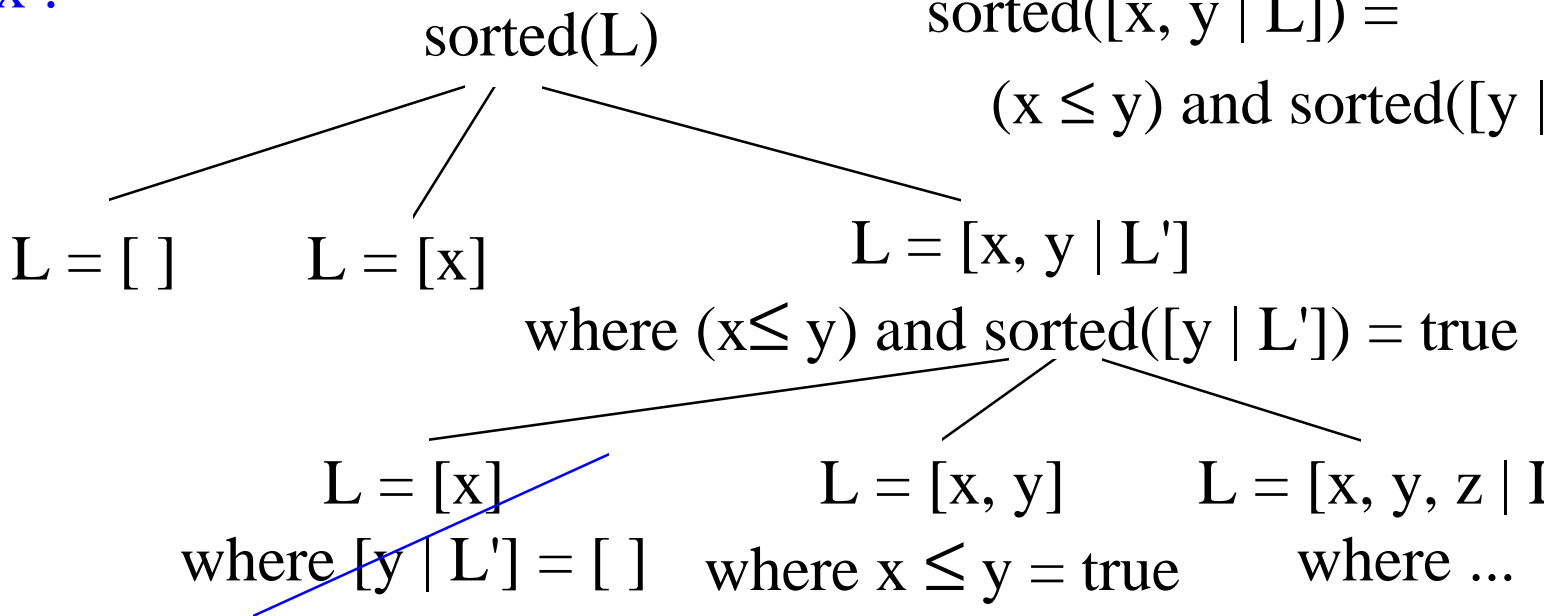


- allows rough subdomain splitting
- quantitative estimate of the future system with an operational profile
- quantitative estimate of the exceptional behaviour with other criteria
- formal specification & domain description
 - ➔ automatic test generation

Deterministic testing

■ cover the definitions case by case

ex :



sorted([]) = true

sorted([x]) = true

sorted([x, y | L]) =

(x ≤ y) and sorted([y | L])

To automate deterministic testing



- solve constraints for each domain
- generate any one value in the domain
 - ➔ use constraint solving methods
(logic programming techniques)

Advantages of deterministic testing



- automate current practice of functional testing
- allows thin subdomain splitting
 - ➔ automatic coverage of exceptional cases
- extracts the oracle from the specification
- opens the door to a standardization of functional coverage criterias

Application to the Lustre language



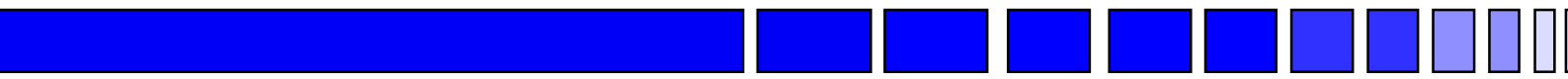
Lustre is a functional and dataflow language
a Lustre node as a cyclic behavior

```
node mem(On : bool ; Of : bool ; Init : bool)  
returns (Out : bool) ;
```

```
    out = if On then (true)  
          else (if Of then (false)  
                else ((Init) → (pre(Out)))) ;
```

```
;
```

Coverage criteria

- 
- coverage on the last cycle
 - ➔ one stream values per test case
 - $A = \text{if } B \text{ then } C \text{ else } D$
 - 2 cases: $B = (\dots, \text{true})$
 $B = (\dots, \text{false})$
 - $A = B \rightarrow C$
 - 2 cases: last cycle = first cycle
last cycle = further cycle

Coverage criteria

to cover all operators :

```
Out = if On then (true)
      else (if Of then (false)
            else ((Init) → (pre(Out)))) ;
```

produces 4 test cases:

mem((..., true), (..., _), (..., _)) = (..., true)

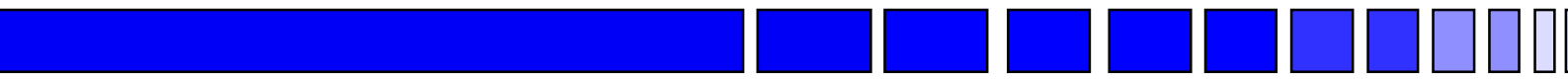
mem((..., false), (..., true), (..., _)) = (..., false)

mem((false), (false), (V)) = (V)

mem((..., _, false), (..., _, false), (..., _, _)) = (..., V, V)

LOFT, a test generator

(developed by B. MARRE)

- 
- on one component:
 - 1386 lines of Lustre
 - 13 nodes
 - 101 inputs and 1 output
 - 2 different selection criterias
 - 982 test cases generated in 20 s. per case
 - 33 test cases generated in 35 s. per case
 - no limit to the test quality

Conclusion



Formals specifications allow to automate testing activities, including Oracle.

- functional probabilistic testing becomes reachable
- deterministic testing automate current empirical methods